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Magnetic tunnel junctions with an equiatomic quaternary CoFeMnSi Heusler alloy electrode
Atomic disorder induced modification of magnetization in MnCrVAl

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We have investigated the physical mechanism behind magnetization reduction in a potential spin-gapless semiconducting compound MnCrVAl by analyzing various atomic disorder schemes. In particular, we show that depending on the degree of disorder, exchanging atomic positions between Mn/Cr and V/Al leads to reduced total magnetization due to either spin flip, or vanishing spin magnetic moments. The latter is attributed to the itinerant character of magnetism in Cr-, Mn-, and V-containing Heusler alloys, and to the frustration of antiferromagnetic exchange interactions, and is accompanied by a tetragonal distortion, but such distortion alone (i.e., in a fully ordered crystal, with no atomic disorder) is not sufficient for a transition to zero magnetization. Besides, we demonstrate that in certain disordered structures the spin polarization of MnCrVAl significantly increases, reaching the half-metallic state. Our calculations indicate that exchange of atomic positions of Mn with Cr, and V with Al has no significant effect on electronic and magnetic properties of MnCrVAl. We also show that antisite disorder does not result in significant reduction of magnetization. At the same time, some types of antisite disorder result in essentially 100% spin-polarized structures. These findings may contribute to understanding the role of atomic disorder on magnetic properties of materials with potential applications in spin-based electronics. Published by AIP Publishing. https://doi.org/10.1063/1.4998308

I. INTRODUCTION

Research on magnetic materials for potential applications in spin-based electronics is one of the most active fields of current study in both academia and industry.1–6 In particular, magnetic materials which can produce highly spin polarized current (ideally, of only one spin orientation, in which case they are called half-metals) attracted enormous attention. Many compounds exhibiting high degree of transport spin polarization have been proposed.7–10 Although experimental confirmation of half-metallicity is rather challenging, it has been shown using spin-polarized positron-annihilation11,12 and infrared absorption13 that a semi-Heusler compound NiMnSb is a half-metal. Additionally, there are various mechanisms which could potentially alter the degree of transport spin polarization, such as mechanical strain, structural disorder, temperature, termination surface/interface in thin film multilayer geometry, etc. For example, it has been shown that segregation of atoms to the surface and emergence of surface states in thin film geometry produce detrimental effects on half-metallic properties.14–21

The main purpose of the current work is to investigate the effect of atomic disorder on the magnetic properties of MnCrVAl, which has recently been investigated as a potential spin-gapless semiconducting (SGS) compound.22,23 Spin-gapless semiconductors are recently discovered materials which are characterized by a zero band gap in one spin channel and a finite band gap in the other channel.24–26 In SGS, not only electrons but also holes are 100% spin polarized and the spin-polarized electron conduction can be tuned between p-type and n-type by adjusting the gate voltage. SGS properties have been reported in oxides such as Co doped PbPdo2, and some Heusler alloys, such as Mn2CoAl, CoCrFeAl, etc.25,26 In our recent work, we demonstrated that in certain materials spin gapless semiconductivity could be induced by atomic substitution with the change in lattice parameters.10

MnCrVAl belongs to the family of full Heusler compounds which crystallizes in a Y-structure (prototype LiMgPdSn) where V and Al occupy the Wyckoff’s 4a and 4b positions, respectively, while Mn and Cr atoms alternate occupy the 4b and 4d sites, which are all located in the middle of the bcc unit cells [see Fig. 1(a)]. In the completely ordered Y-structure, this material is theoretically predicted to be nearly SGS with net magnetic moment of ≈3.0 μB/f.u.27 However, in our recent experimental work, we showed that MnCrVAl samples exhibit close to zero value of net magnetization.23 Here, we present detailed theoretical study of the physical mechanism responsible for the quenching of magnetic moment in this material. In particular, we show that certain states of experimentally observed atomic disorder result in vanishing spin magnetic moments.

The paper is organized as follows: In Sec. II, we present computational methods. In Sec. III, we outline our main results on electronic, magnetic, and structural properties of ordered and disordered MnCrVAl, with various possible combinations of atomic disorder. In Sec. IV, we discuss the results and summarize the paper.

II. METHODS

We performed density functional theory (DFT) calculations of bulk Heusler compound, MnCrVAl using the projector augmented-wave method (PAW),28 implemented in the Vienna  \textit{ab initio} simulation package (VASP)29 within the
generalized-gradient approximation (GGA).\textsuperscript{30} The integration method,\textsuperscript{31} with a 0.05 eV width of smearing was used, along with the plane-wave cut-off energy of 500 eV and convergence criteria of 10\(^{-5}\) eV for atomic relaxation, and 10\(^{-3}\) meV for the total energy and electronic structure calculations. A \(k\)-point mesh of 12\(^{1/2}\) \(\times\) 12\(^{1/2}\) \(\times\) 12 was used for the Brillouin-zone integration. The atomic arrangement of fully ordered 16-atom cubic unit cell used in our calculation is shown in Fig. 1(a). Here, V and Al occupy the Wyckoff’s 4a and 4b positions, respectively, while Mn and Cr atoms occupy the 4b and 4d sites, which are all located in the middle of the bcc unit cell. To simulate atomic disorder, we interchanged atomic positions of different elements, as explained in the text below. For all ground state calculations, the lattice parameters were fully optimized to obtain equilibrium structures. Periodic boundary condition was imposed in all calculations. Some of the results were obtained using the MedeA\textsuperscript{\textregistered} software environment.\textsuperscript{32}

III. RESULTS AND DISCUSSION

A. Ideal structure

Figure 1(a) shows the unit cell of the completely ordered MnCrVAl. The calculated optimal lattice constant is 5.90 Å. Figure 1(b) shows calculated densities of states (DOS) of this material at the ground state. Aside from a very small contribution from Mn and Cr atoms (which could be a computational artefact due to the energy width of smearing), the majority-spin DOS is essentially zero at the Fermi level with band gap of \(\approx\)0.5 eV. Further, the minority-spin DOS demonstrates a tendency towards gapless semiconducting behavior consistent with the previous report.\textsuperscript{27} As one can see from the Fig. 1(b), the maximum of the minority-spin valence band is mostly composed of Mn states, while the minimum of the unoccupied minority-spin states has comparable contribution from Mn, Cr, and V.

The calculated magnetic structure of MnCrVAl in the ground state is ferrimagnetic, with net magnetic moment of 2.90 \(\mu_B\)/Eu. The atomic contributions are 1.776 \(\mu_B\), 2.077 \(\mu_B\), and \(-0.943 \mu_B\) per Mn, Cr, and V correspondingly (see Table I). As mentioned earlier, this result is in contrast with our recently published experimental work where the arc-melted samples of MnCrVAl showed almost zero net magnetic moment.\textsuperscript{23} Our XRD measurements indicated a significant degree of atomic disorder in the samples.\textsuperscript{23} Here, we analyze how the magnetic, electronic, and structural properties of this material change as various disordered states are considered.

B. Effect of swap disorder

To investigate possible effects of atomic disorder on magnetic properties of MnCrVAl, we constructed various cells of this alloy by interchanging atomic position in 16-atom unit cell, as shown in Fig. 2. Here, Mn1-Al1 notation indicates that the positions of Mn1 and Al1 atoms [see Fig. 1(a) for numbering of the atoms] have been interchanged, Mn1, 2-Al1, 2 indicates that positions of Mn1 and Al1, and at the same time positions of Mn2 and Al2 are interchanged. All other disordered cells are labeled in the similar manner. Each of the structures was fully optimized. The calculated lattice parameters are presented in the Table I.

Table I summarizes the calculated magnetic moments for each of the structures shown in Fig. 2. One can see that atomic disorder in all the states except Cr1-V1 results in reduced magnetization (for Mn1-V1 this reduction is very small, but not negligible). Moreover, there are three instances of vanishing magnetization: Mn1,2-Al1,2, Mn1,2-V1,2, and Cr1,2-Al1,2. In these three cases, the zero magnetization transition is accompanied by a cubic to tetragonal distortion, which is more pronounced in Mn1,2-V1,2. The last column of the Table I shows formation energies of the disordered structures, calculated as a total energy difference of ordered and disordered cell, i.e., less negative value indicates more stable structure. One can see that of the three disordered structures with zero magnetization, the highest formation energy (i.e., the least negative value) corresponds to Cr1,2-Al1,2 disorder, while the second least negative value corresponds to Mn1,2-Al1,2 disorder. The formation energy of
Mn1,2-V1,2 is significantly higher ($E_{\text{formation}}$ is more negative). In all considered cases, the ordered structure corresponds to the lowest energy state. As discussed in Ref. 23, the XRD measurements indicate a significant degree of atomic disorder in the samples, which could be caused by various reasons, e.g., preparation methods. We therefore argue that experimentally observed zero magnetization in MnCrVAl could result from atomic swap disorder, possibly of Cr1,2–Al1,2 and Mn1,2–Al1,2 type.

Next, we look at the electronic structure of disordered cells. Figures 3 and 4 show atom- and spin- resolved densities of states of the cells with Mn-type and Cr-type (interchange of Mn atoms and Cr atoms correspondingly) atomic disorder. As shown in Figs. 3(c) and 3(d) and Fig. 4(c), Mn1,2–Al1,2, Mn1,2–V1,2, and Cr1,2–Al1,2 disordered cells exhibit non-spin-polarized electronic structure, corresponding to vanishing spin magnetic moments. In particular, as a result of atomic disorder in these structures, new states emerge near Fermi level, mostly of Mn, Cr, and V character (with comparable contribution from all three elements). These states essentially cancel out the spin polarization. The other five disordered cells demonstrate various degrees of non-zero spin-polarization, which is especially pronounced for Cr1–Al1 disorder, which exhibits a nearly half-metallic electronic structure.

All three non-magnetic disordered cells exhibit tetragonal distortion; see the second column of the Table I. It is important to understand if the tetragonal distortion without atomic disorder can induce the transition to zero magnetization. In order to find an answer to this question, we performed calculations for a fully ordered MnCrVAl, under both compressive and tensile strain. For the former, we set the in-plane lattice constant to 5.80 Å, while for the latter we set it to 6.00 Å (i.e., 1.7% off the cubic ground state value). In both cases, the out-of-plane lattice parameter was fully relaxed, with the optimal values of 5.966 Å for compressive, and 5.817 Å for tensile strain. In both cases, magnetic and electronic structures are not significantly different from the corresponding structures of the fully ordered cubic cell, i.e., the spin magnetic moments

<table>
<thead>
<tr>
<th>Lattice (a/b/c)</th>
<th>Mn1</th>
<th>Mn2,3,4</th>
<th>Cr1</th>
<th>Cr2,3,4</th>
<th>V1</th>
<th>V2,3,4</th>
<th>Al1</th>
<th>Al2,3,4</th>
<th>Total</th>
<th>$E_{\text{formation}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ordered</td>
<td>5.90/5.90/5.90</td>
<td>1.776</td>
<td>1.776</td>
<td>2.077</td>
<td>2.077</td>
<td>-0.943</td>
<td>-0.943</td>
<td>-0.007</td>
<td>-0.007</td>
<td>11.610</td>
</tr>
<tr>
<td>Mn1-Al1</td>
<td>5.88/5.88/5.88</td>
<td>-1.741</td>
<td>1.632</td>
<td>1.189</td>
<td>1.716</td>
<td>-1.007</td>
<td>-0.864</td>
<td>-0.018</td>
<td>-0.012</td>
<td>5.840</td>
</tr>
<tr>
<td>Mn1-V1</td>
<td>5.91/5.91/5.91</td>
<td>-2.204</td>
<td>1.950</td>
<td>2.021</td>
<td>1.975</td>
<td>0.961</td>
<td>-0.901</td>
<td>-0.003</td>
<td>0.010</td>
<td>9.880</td>
</tr>
<tr>
<td>Mn1,2-Al1,2</td>
<td>5.84/5.77/5.84</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td>Mn1,2-V1,2</td>
<td>6.04/5.73/5.73</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
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<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td>Cr1-Al1</td>
<td>5.87/5.875.87</td>
<td>1.122</td>
<td>1.694</td>
<td>-1.359</td>
<td>1.600</td>
<td>-1.077</td>
<td>-0.837</td>
<td>-0.030</td>
<td>-0.013</td>
<td>5.99</td>
</tr>
<tr>
<td>Cr1-V1</td>
<td>5.90/5.87/5.87</td>
<td>1.911</td>
<td>1.836</td>
<td>-1.303</td>
<td>2.105</td>
<td>1.558</td>
<td>-0.891</td>
<td>-0.005</td>
<td>0.008</td>
<td>11.34</td>
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<tr>
<td>Cr1,2-Al1,2</td>
<td>5.78/5.78/5.91</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td>Cr1,2-V1,2</td>
<td>5.91/5.90/5.91</td>
<td>-0.522</td>
<td>1.558</td>
<td>-0.528</td>
<td>-0.528</td>
<td>-0.357</td>
<td>-0.523</td>
<td>0.005</td>
<td>0.010</td>
<td>1.88</td>
</tr>
</tbody>
</table>

Compressive

<table>
<thead>
<tr>
<th>Lattice (a/b/c)</th>
<th>Mn1</th>
<th>Mn2,3,4</th>
<th>Cr1</th>
<th>Cr2,3,4</th>
<th>V1</th>
<th>V2,3,4</th>
<th>Al1</th>
<th>Al2,3,4</th>
<th>Total</th>
<th>$E_{\text{formation}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Compressive</td>
<td>5.8/5.8/5.966</td>
<td>1.720</td>
<td>1.720</td>
<td>2.051</td>
<td>2.051</td>
<td>-0.880</td>
<td>-0.880</td>
<td>-0.003</td>
<td>-0.003</td>
<td>11.55</td>
</tr>
<tr>
<td>Tensile</td>
<td>6.0/6.0/5.817</td>
<td>1.849</td>
<td>1.849</td>
<td>2.105</td>
<td>2.105</td>
<td>-1.022</td>
<td>-1.022</td>
<td>-0.013</td>
<td>-0.013</td>
<td>11.68</td>
</tr>
</tbody>
</table>

FIG. 2. Crystal structures of disordered MnCrVAl.
are not vanishing. The last two rows in Table I show the calculated magnetic moments of fully ordered cells under compressive and tensile strain, while Fig. 5 shows the calculated densities of states of these two structures. Comparison of Figs. 1(b) and 5(a), 5(b) shows that the electronic structure of MnCrVAl is not very sensitive to the external strain, as both total and atom-projected DOS exhibit similar features under zero and positive/negative compression.

To better illustrate the nature of the atomic disorder induced magnetization modification in MnCrVAl, we plot average planar magnetization density in the unit cell of fully ordered and disordered structures (see Fig. 6). In Fig. 6, the two positive magnetization peaks correspond to \(z = 0.25\) and \(z = 0.75\) (direct coordinates). This corresponds to two planes which contain Mn and Cr atoms in the fully ordered unit cell [see Fig. 1(a)]. The negative peaks correspond to \(z = 0.0\), \(z = 0.5\), and \(z = 1.0\), i.e., planes containing Al and V atoms in
the ordered cell, and result from the spin-down orientation of the magnetic moment of vanadium. (Note that Fig. 6 shows distance in z-direction in Cartesian (not direct) coordinates.) As one can see, Cr1-V1 and Mn1-V1 atomic disorders do not significantly change magnetization density in the cell [compare black and red lines in Figs. 6(a) and 6(b)]. At the same time, Cr1-Al1 and Mn1-Al1 disorders result in nearly identical modification of the magnetization density profile, which reduces approximately twice the total magnetization. Except Cr1,2–V1,2, all disordered cells with interchange of two atoms exhibit zero magnetization density. Cr1,2–V1,2 disorder also results in a strong suppression of the total magnetization density [gray line in Fig. 6(a)], which, however, is not vanishing. Overall, magnetization suppression is much stronger when atomic positions of Cr/Mn are interchanged with Al than with V. This is likely due to the strong hybridization between non-spin polarized states of Al with spin-polarized states of Cr/Mn when positions of Al and Cr/Mn are interchanged, which results in magnetization quenching. On the other hand, when Cr/Mn positions are interchanged with V, the magnetization reduction is less pronounced, since both V and Cr/Mn states are spin-polarized and their increased overlap has a smaller effect on magnetization profile.

Finally, we also performed atomic disorder calculations with the exchange of atomic positions of Mn with Cr, and V with Al. This type of disorder has no significant effect on the electronic and magnetic properties of MnCrVAl, i.e., both magnetic and electronic structures show no noticeable deviation from that of the fully ordered cell.

C. Effect of antisite disorder

Recently, Feng et al. demonstrated that along with the swap disorder, antisite disorder may also have an important effect on the electronic and magnetic properties of some Heusler alloys. To investigate the effect of the antisite disorder on MnCrVAl, we constructed supercells of 32 atoms. In ordered structure, there are 8 atoms of each element. We consider all 12 possible types of antisite disorder: Al(Cr), Al(Mn), Al(V), Cr(Al), Cr(Mn), Cr(V), Mn(Al), Mn(Cr), Mn(V), V(Al), V(Cr), and V(Mn). In each of these 12 structures, one of the atoms of the element shown in parentheses is replaced with an atom preceding parenthesis [e.g., one
atom of Cr is replaced with Al in Al(Cr)]. The calculated magnetic moments are summarized in Table II. One can see that all antisite disorder structures exhibit large magnetization. We therefore conclude that experimentally observed quenching of magnetization cannot result from antisite disorder. Calculated densities of states of all 12 structures with antisite disorder are shown in Fig. 7. One can see that while all of these disorders result in additional minority-spin states around Fermi level, yet some of these structures [Al(Cr), Al(Mn), Cr(Mn), and V(Cr)] exhibit nearly perfect half-metallicity and therefore could have practical applicability.

IV. DISCUSSION AND CONCLUSIONS

Our calculations indicate that atomic disorder induced decrease in the total spin magnetic moment in MnCrVAl is due to two physical mechanisms: induced antiferromagnetic exchange interaction (spin flip) and vanishing of the atomic spin moments. The latter is likely responsible for the experimentally observed zero magnetization in this alloy.23 The atomic disorder induced antiferromagnetic coupling is Mn/Cr/V atoms could be due to the increased overlap of the corresponding d orbitals, which results from reduced interatomic distances.34,35 At the same time, vanishing of the atomic spin moments in Mn1,2–Al1,2, Mn1,2–V1,2, and Cr1,2–Al1,2 disordered cells is probably due to a subtler mechanism. In particular, a similar reduction of the spin magnetic moment in another Heusler material, Cr3Se has been reported by Galanakis et al., and was attributed to the metamagnetic behavior of this material, i.e., coexistence of itinerant and localized spin magnetic moments.36 It is plausible to suggest that a similar mechanism may be responsible for the vanishing spin moments in disordered MnCrVAl. First, Cr-, Mn-, and V-containing Heusler alloys are likely to exhibit itinerant magnetism, and second, the disorder induced cell compression is comparatively small (see Table I), and is more likely to induce antiferromagnetic coupling than to reduce the atomic spin moments.

<table>
<thead>
<tr>
<th></th>
<th>Al(Cr)</th>
<th>Al(Mn)</th>
<th>Al(V)</th>
<th>Cr(Al)</th>
<th>Cr(Mn)</th>
<th>Cr(V)</th>
<th>Mn(Al)</th>
<th>Mn(Cr)</th>
<th>Mn(V)</th>
<th>V(Al)</th>
<th>V(Cr)</th>
<th>V(Mn)</th>
</tr>
</thead>
</table>

FIG. 7. Calculated total densities of states of the structures with antisite disorder. Positive DOS corresponds to majority-, negative DOS to minority- spin states.
very unlikely to result in disappearance of the spin moments, if these moments are strongly localized (itinerant magnetic moments are reduced significantly faster). See Refs. 36 and 37 for further discussion of metamagnetism in Heusler alloys.

Results presented in this work are in overall agreement with our recent experimental study. In particular, in our experimental work, we used XRD measurements to show that MnCrVAl samples that exhibit zero magnetization have very strong A2-type disorder, which corresponds to the Mn-Al and Cr-Al atomic swap. At the same time, our XRD measurements did not indicate any B2-type atomic disorder, which corresponds to the V-Al atomic swap. This is consistent with our first-principles results, which indicate that while A2-type disordered cells exhibit reduced magnetization, B2-type disorder does not significantly affect magnetic structure of the cell.

In conclusion, we showed that atomic swap disorder in MnCrVAl mostly results in either reduced total magnetization due to spin flip or in vanishing spin magnetic moments. The latter is accompanied by a tetragonal distortion, while all disordered cells with non-zero magnetization are cubic. Further, we also showed that tetragonal distortion alone (with no atomic disorder) is not sufficient for a suppression of magnetization. Besides, we demonstrated that although atomic disorder typically results in reduced spin-polarization of MnCrVAl, yet in certain disordered structures (Cr1–Al1) the spin polarization is very high, almost reaching the half-metallic state. Our calculations indicate that exchange of atomic positions of Mn with Cr, and V with Al has no significant effect on electronic and magnetic properties of MnCrVAl. We also showed that while antisite disorder does not result in significant reduction of magnetization, yet some types of this disorder may result in nearly 100% spin-polarized structures. Finally, although not considered in this work, but frustrated exchange interactions in some forms of A2-type atomic disorder may result in non-collinear magnetic structure, potentially exhibiting magnetic vortices (skyrmions). Reliable study of this effect using standard DFT techniques would be computationally very demanding, but may be an interesting subject of future investigation. Another potentially interesting topic of future study is magnetic domain structure of MnCrVAl and, in particular, its response to atomic disorder. Such an investigation, however, would also require beyond standard DFT methods. Overall, we hope that our findings are important for understanding the effect of atomic disorder on magnetic properties of materials with potential applications in spintronics.

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